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In [1]: from sympy import *
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Example 1: Solve the ODE $y'' + 3y' + 2y = 0$.

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In [2]: #Using the technique discussed in class:
t=symbols('t')
y=Function('y')
dsolve(diff(y(t),t,2)+3*diff(y(t),t)+2*y(t),y(t)) #Note that expanding it g
ives the same solution as in class
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Out[2]:  $y(t) = (C_1 + C_2e^{-t}) e^{-t}$ 
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Example 2: Solve the IVP $y'' + y' - 6y = 0$, $y(0)=1$, $y'(0)=2$

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In [3]: # Using dsolve and ics option
t=symbols('t')
y=Function('y')
ysoln=dsolve(diff(y(t),t,2)+diff(y(t),t)-6*y(t),y(t),ics={y(0):1,diff(y(t),
t).subs(t,0):2})
# NOTICE how y'(0) has to be entered. y is a FUNCTION, but diff(y(t),t) is
an expression which requires substitution
print(ysoln)
```

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Eq(y(t), exp(2*t))
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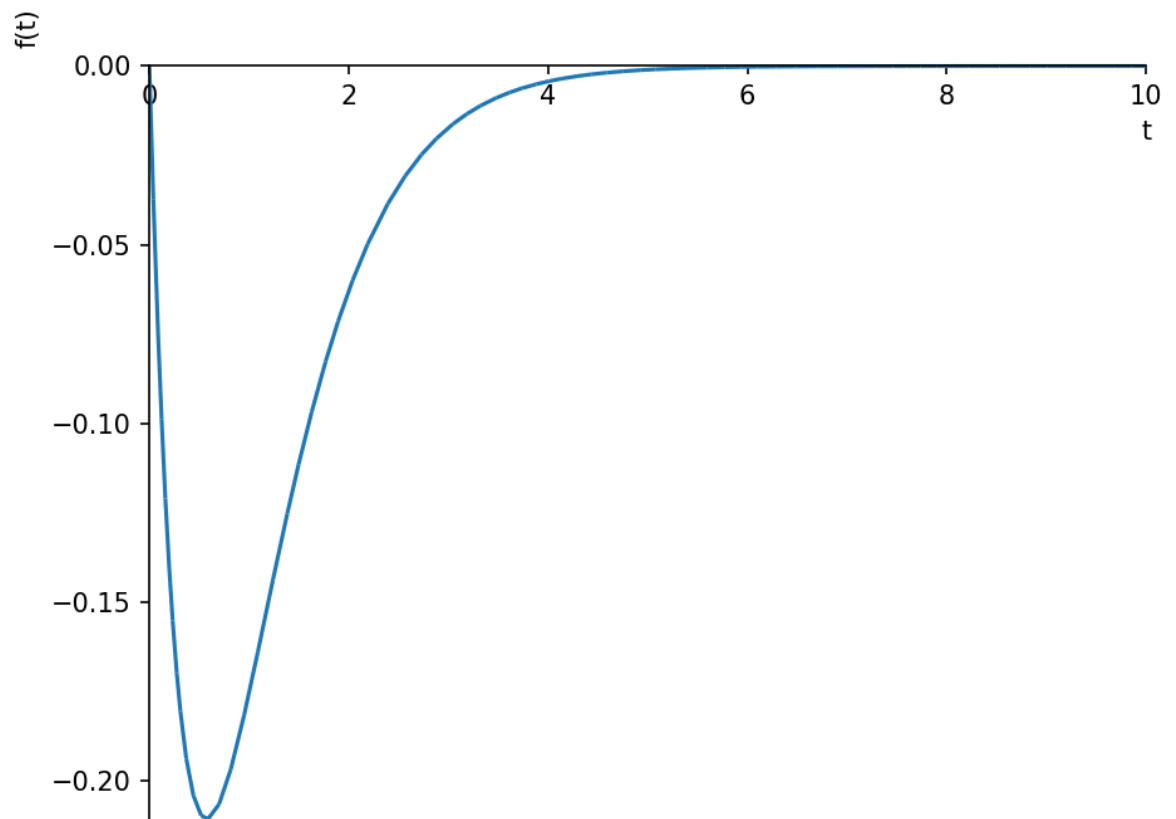
Example 3: Solve the IVP $2y''+7y'+6y = 0$, $y(0) = 0$, $y'(0) = -1$

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In [5]: t=symbols('t')
y=Function('y')
ysoln=dsolve(2*diff(y(t),t,2)+7*diff(y(t),t)+6*y(t),y(t),ics={y(0):0,diff(y
(t),t).subs(t,0):-1})
print('The solution to the IVP is',ysoln)
# NOTE that by properties of exponents,  $e^{t^{3/2}} = e^{(3/2)t}$ 
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Eq(y(t), 2*exp(-2*t) - 2/exp(t)**(3/2))
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In [7]: matplotlib notebook
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In [9]: yoft=ysoln.rhs
plot(yoft,(t,0,10))
print('Note  $y \rightarrow 0$  as  $t \rightarrow \infty$  which makes sense since both roots are negative.')
e.'
```



Note $y \rightarrow 0$ as $t \rightarrow \infty$ which makes sense since both roots are negative.

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In [ ]:
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