3.4: Repeated Roots and Reduction of Order

Examples: y'' + 2y' + y = 0

Solve the IVP 4y'' + 4y' + y = 0, y(1) = 1, y'(1) = 1. Describe the behavior of the solution as t increases.

Show that $y_1 = t$ is a solution to the ODE $t^2y'' + 2ty' - 2y = 0$, t > 0. Find a second solution y_2 and verify that y_1 and y_2 form a fundamental set of solutions.