

```
In [1]: from sympy import *
```

Example 1: $y'' + 2y' + 10y = \delta(t-5)$, $y(0)=y'(0)=0$

(The command is DiracDelta(t-c))

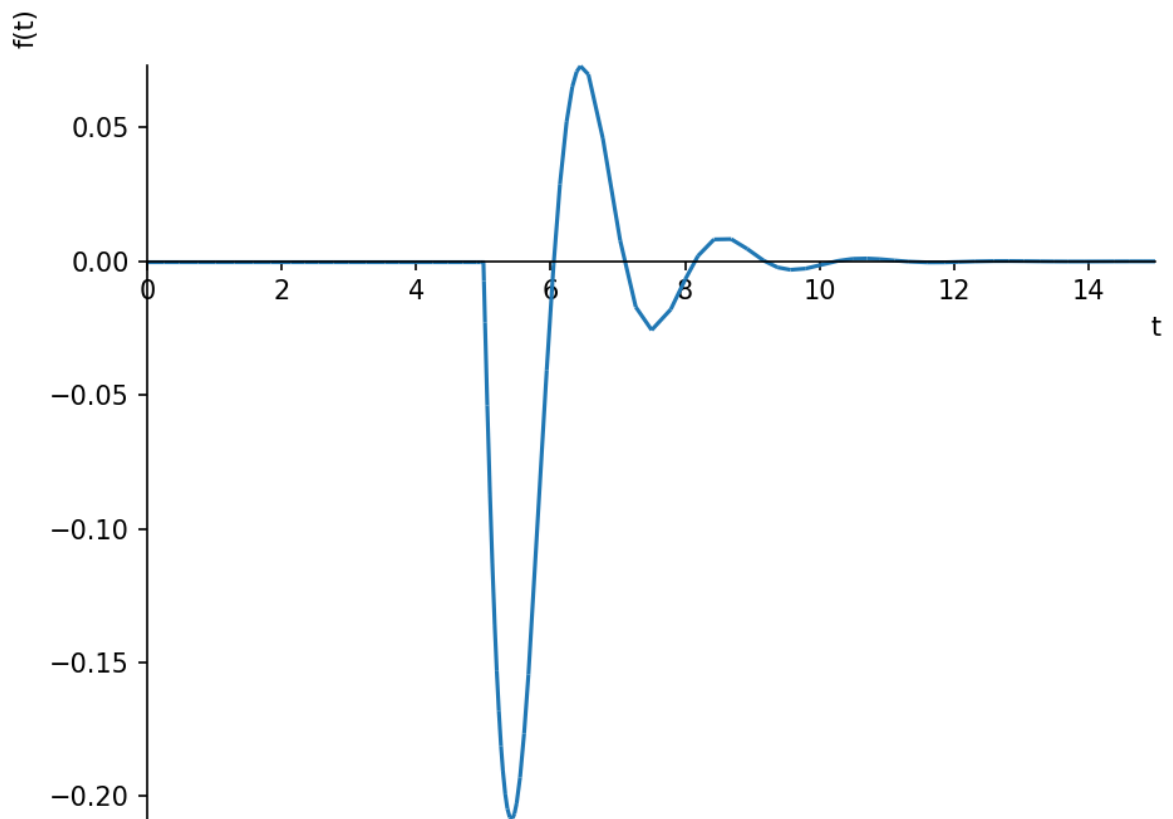
```
In [2]: t=symbols('t')
y=Function('y')
g=DiracDelta(t-5)
deq=diff(y(t),t,2)+2*diff(y(t),t)+10*y(t)-g
ysoln=dsolve(deq,y(t),ics={y(0):0,diff(y(t),t).subs(t,0):0})
print('The solution is',ysoln)
```

The solution is Eq(y(t), exp(5)*exp(-t)*sin(3*t - 15)*Heaviside(t - 5)/3)

Again I will plot the solution to help visualize the motion

```
In [3]: matplotlib notebook
```

```
In [7]: y=ysoln.rhs
# NOTE: Since we call down "positive", I am multiplying the solution by -1
to visualize this fact
plot(-1*y,(t,0,15))
```



```
Out[7]: <sympy.plotting.plot.Plot at 0x7ccd9b0>
```

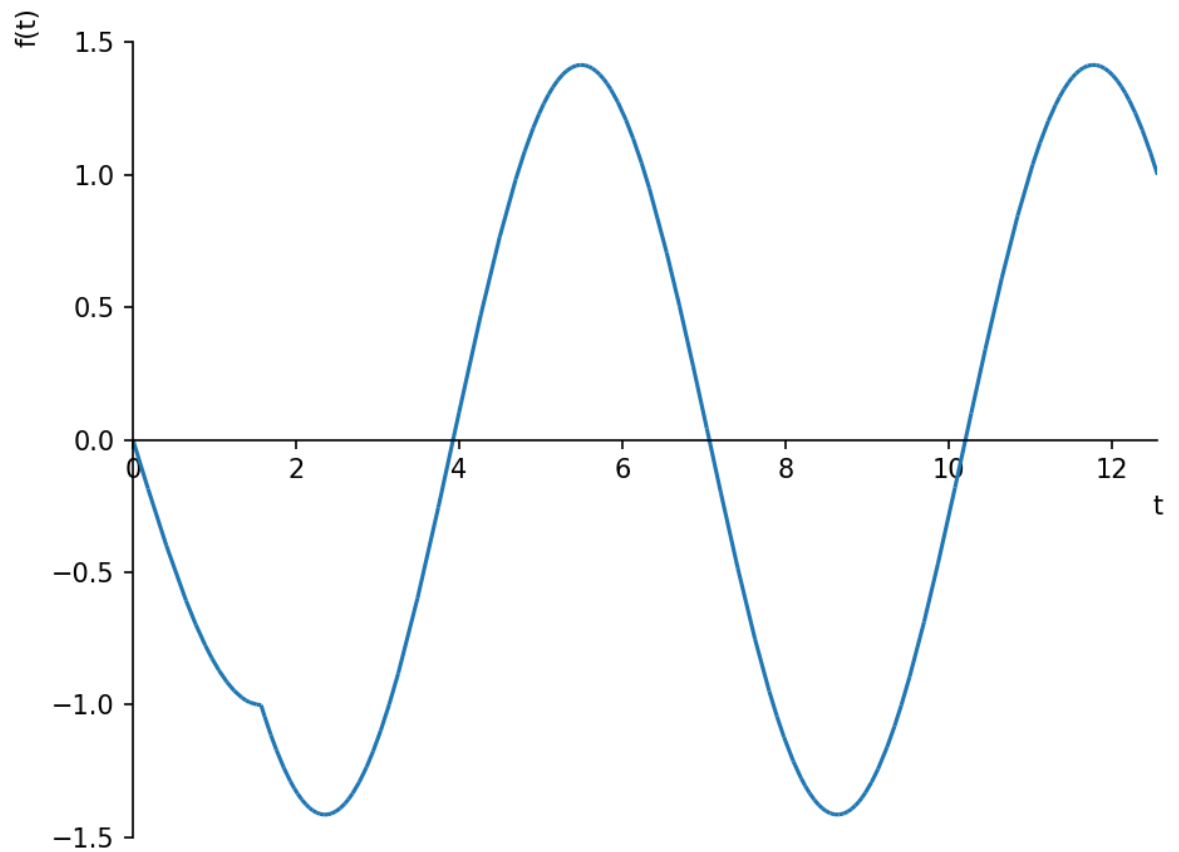
Example 2: $y'' + y = \delta(t - \pi/2)$, $y(0)=0$, $y'(0)=1$

```
In [10]: t=symbols('t')
y=Function('y')
g=DiracDelta(t-pi/2)
deq=diff(y(t),t,2)+y(t)-g
ysoln=dsolve(deq,y(t),ics={y(0):0,diff(y(t),t).subs(t,0):1})
print('The solution is',ysoln)
print('NOTE: in one class, it was pointed out that sin(t-pi/2) = -cos(t) so
the answer is equivalent to ours.')
```

The solution is $\text{Eq}(y(t), \sin(t) - \cos(t) \cdot \text{Heaviside}(t - \pi/2))$
NOTE: in one class, it was pointed out that $\sin(t - \pi/2) = -\cos(t)$ so the answer is equivalent to ours.

```
In [11]: matplotlib notebook
```

```
In [13]: y=ysoln.rhs  
plot(-1*y,(t,0,4*pi))
```



```
Out[13]: <sympy.plotting.plot.Plot at 0xa0f7ed0>
```

```
In [ ]:
```