Choosing $r$ objects from $n$ objects,
or, Putting $r$ objects into $n$ boxes

|  | Repetition | No repetition |
| :---: | :---: | :---: |
| Ordered/ Distinguishable | Sequences (Arrangements) | Permutations |
|  | $n^{r}$ | $P(n, r)=\frac{n!}{(n-r)!}$ |
|  | Table-service order | Choosing seats |
|  | Maxwell-Boltzmann particles | - |
| Unordered/ Indistinguishable | Combinations with repetition (Multisets) | Combinations (Subsets) |
|  | $\binom{n-1+r}{r}=\frac{(n-1+r)!}{r!(n-1)!}$ | $C(n, r)=\binom{n}{r}=\frac{n!}{r!(n-r)!}$ |
|  | Fast-food order | Setting the table |
|  | Bose-Einstein particles | Fermi-Dirac particles |

## References:

1. M. Townsend, Discrete Mathematics: Applied Combinatorics and Graph Theory, Benjamin/Cummings, Menlo Park, 1987, Sec. 2.3.
2. Grimaldi, 4th ed., Secs. 1.4 and 1.7.
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